



## Advanced Modal Analysis

This course focuses on additional test and analysis tools beyond those presented in the Basic Modal Analysis course. Topics include operating data, multiple input multiple output testing, advanced multiple reference modal parameter estimation, structural dynamic modification using both modal data and measured impedances, forced response simulation, and other topics related to advanced manipulation of measured structural dynamic data.

- First, the basics of Basic Modal Analysis and applicable engineering fundamentals are discussed to gain a common understanding of the application and general principles are reviewed.
- Next, participants will focus on further developing their skills beyond Basic Modal Analysis.
- Lastly, participants will be shown how to run the model and interpret output results on LMS software products. A thorough understanding of what these results mean and how to use them to improve the product design will be discussed.



## Course Syllabus

### I IDENTIFYING INFORMATION

<b>Course:</b>	Advanced Modal Analysis
<b>Prerequisite:</b>	Experimental Modal Analysis
<b>Time Frame:</b>	40 total contact hours
<b>Instructor:</b>	Dr. Peter Avitabile Director of the Modal Analysis and Controls Laboratory BS in Mechanical Engineering MS in Mechanical Engineering PhD in Mechanical Engineering 25 years at UMASS Lowell Professor Mechanical Engineering 10 years industrial experience in structural dynamics, modeling and design
<b>E-mail:</b>	<a href="mailto:Peter.Avitabile@uml.edu">Peter.Avitabile@uml.edu</a>

### II REFERENCE MATERIALS

1. The Fundamentals of Signal Analysis (Hewlett Packard App Note 243)
2. Fundamentals of Modal Analysis (Hewlett Packard App Note 243-3)
3. Experimental Modal Analysis - A Simple Non-Mathematical Overview  
Modal Space articles originally published in Experimental Techniques

### III COURSE GOALS AND OBJECTIVES

1. Understand the steps in the development of an experimental model
2. Understand the considerations for the test beyond a basic simplistic test
3. Understand SDOF and MDOF models and modal space concepts
4. Understand the need for windowing and its effects
5. Know and understand the basic and advanced measurements needed
6. Understand and be able to apply impact and shaker excitation techniques
7. Understand multiple input multiple output employed in modal testing
8. Understand tools used for identification of modes
9. Understand and be able to validate experimental modal models
10. Understand the structural dynamic modification and modeling approaches utilizing reduced order models, modal models and frequency response
11. Understand the collection of operating data and extraction methods for development of a modal model from output only system measurements



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12. Understand the forced response simulation procedures using modal data
13. Understand how to apply advanced linear algebra methodologies in the application for solving advanced structural dynamic modeling
14. Understand the basic approaches for the correlation of measured data with analytical models (such as a finite element model)



#### **IV METHODOLOGY**

This course is an introduction to advanced modal analysis theory and techniques that are used to characterize the dynamic characteristics of structures. Each module will introduce new material that the student will be allowed to experience for himself with the associated exercises.

##### **Lectures**

Each detailed subject will be presented in a lecture format outlining the theory and standardized accepted methodology. A printed copy of the lecture material will be provided for the student's personal in-class use and as a reference material.

##### **Specific Industry Examples**

Real life examples will be covered that explain the application of the theory to various industries such as automotive, aerospace, home appliance. This will give the students a clear understanding of how and why these techniques are utilized in different industries and the value they add to noise and vibration refinement.

##### **In-Class Assignments**

The student will conduct several hands-on exercises to reinforce the theoretical concepts and to perform advanced analyses. These exercises will increase in complexity as the students further develop their skills in understanding modal theory and practice. Many different data sets are collected as a class and then individual groups are given specific tasks/approaches for the reduction of data; different groups are given different subsets of data to manipulate for operating data collected. The students will present their work to the group for review and discussion. Other more structured lab exercises are also given as individual assignments for the application of SDM, system modeling, forced response simulation, etc.



**V COURSE OUTLINE & ASSIGNMENTS**

**Module 1 – Overview of Structural Dynamic Modeling Techniques**

Modal Analysis and Structural Dynamics  
Analytical Modal Analysis and Finite Element Models  
Experimental Modal Analysis and Experimental Modal Reduction  
Frequency Response Functions (FRFs) and Mode Shapes from FRFs  
Correlation and Updating Models  
Overview of Advanced Applications of Structural Dynamic data

**Module 2 – Review of Basic Modal Analysis Theory and Related Topics**

Different Mathematical Model Formulations  
SDOF and MDOF Theory Overview  
Frequency Response Functions  
Linear Algebra Concepts for Structural Dynamic Applications

**Module 3 – Review of Basic Measurement Definitions**

Linear Spectra and Power Spectra  
Derived Relationships and Effects of Noise – Estimators  $H_1$ ,  $H_2$ ,  $H_v$   
Auto Power and Cross Power Spectrum; Frequency Response Function;  
Coherence

**Module 4 – Review of Basic Impact and Single Shaker Excitation**

Overview Basic Impact Testing Procedures  
Review Multiple Reference Impact Test  
Overview Basic Shaker Testing Approaches & common excitation signals utilized

**Module 5 – Multiple Input Multiple Output Shaker Testing**

Multiple Input Shaker Testing  
Principal Component Analysis  
Multiple and Partial Coherence  
SISO vs. MIMO

**Module 6 – Mode Indicator Techniques**

Review of Identification Functions Typically Employed  
(such as Mode Indicator Function, Multivariate Mode Indicator Function,  
Complex Mode Indicator Function, Stability Diagram and Poly MAX)



### **Module 7 – Basic Modal Parameter Estimation**

Parameter Estimation Concepts and Parameter Extraction Considerations  
Classification of Modes; Time and Frequency Domain Representations  
Different Forms of the Same Equation; Why Have Different Methods  
Modal Parameter Estimation Concepts and Extraction Considerations  
Mode Determination Tools; Model Order; Stability Diagram  
Modal Extraction Methods  
SDOF Modal Parameter Estimation  
MDOF Modal Parameter Estimation  
Modal Parameter Estimation Considerations

### **Module 8 – Modal Parameter Estimation Guidelines and Practical Considerations**

Basic Curve Fitting; Considering Complicated Structures; Curve Fitting Guidelines  
Historical Perspective of Modal Parameter Estimation  
Case study of a very complicated aerospace structure with methodology used to decipher MIMO test results to obtain useful modal parameters

### **Module 9 – Model Validation – Basic and Advanced Tools**

Animation  
Modal Assurance Criteria  
FRF Synthesis  
Modal Participation; Mode Complexity  
Mode Phase Colinearity / Mean Phase Deviation  
Amplitude Weighted Assessment Function with application to Rib Stiffened Plate  
Extended Amplitude Weighted Assessment Function

### **Module 10 – Test Reference Identification Procedure with Applications**

Identification of Reference Locations using Singular Valued Decomposition  
Practical Development of the Test Reference Identification Procedure using SVD  
Rib Stiffened Plate Example; Repeated Root Plate Example; Composite Plate  
Pseudo-Repeated Root Example; Composite Fin Plate Pseudo-Repeated Root  
Example  
Application of TRIP on Large Chiller Unit

### **Module 11 – Additional Topics in Modal Analysis – Advanced Formulations**

Re-visit the Input-Output Frequency Domain Formulation of Dynamic Response  
- Develop the Forced Response Simulation Approach  
- Develop Operating Data Approach – Output Only Systems  
- Develop the Force Estimation from Operating Data



**Module 12 – Operating Deflection Shapes**

Characterization: Time or Frequency Domain

ODS: Time Domain

ODS: Frequency Domain, Linear Spectrums

ODS: Frequency Domain, Transmissibility

ODS: Frequency Domain, Cross Spectrum

ODS: Frequency Domain, Reference Criteria

ODS: Multiple Uncorrelated Sources

ODS: Principal Component Analysis

**Module 13 – ODS Scaling Techniques-**

Overview the Approaches Available for Scaling Operating Data

- Scaling Operating Data using the Drive Point Residue Method

- Scaling Operating Data using the Mass SDM Approach

**Module 14 – Operational Modal Analysis – Practical Examples**

Develop Operating Modal Data from various approaches for Output Only Measurements

**Module 15 – Structural Dynamic Modification**

Types of Models Used in Modification Studies

Real Normal Modes or Complex Modes

Modal Space Models or Impedance Models

Simplistic Modifications or Realistic Modifications

Structural Dynamic Modification and System Modeling

Truncation Effects and Rotational Degrees of Freedom Considerations

**Module 16 – Frequency Based Sub Structuring**

Formulate the Impedance Modeling Approach for a Single Modification (SMURF)

Formulate the Impedance Modeling Approach for Multiple Modifications (FBS)

**Module 17 – Effects of Rotational DOF for Impedance Modeling Applications**

Identify the Important of Rotational Measurements in Practical SDM and System Modeling Applications



**Module 18 – Test-Analysis Correlation-Updating Considerations -**

Identify the basic tools used for test-analysis correlation

Discuss vector based and DOF based approaches

Identify the various correlation tools such as MAC, CoMAC, POC, FRAC, RVAC

Exercises-

Modal Parameter Estimation

Operational Modal Analysis

Modification of a Free-Free Beam

Structural Modification of a Support Beam with a Tuned Absorber

Combining Modal Beam and Support Beam

Coupling of Modal Beam and Support Beam Using FRF's